

FRACTIONS, ADDITION & SUBTRACTION

FACT 1: We add and subtract like fractions, by adding and subtracting numerators.

$$\frac{1}{4} + \frac{2}{4} = 1 \text{ of } \frac{1}{4} + 2 \text{ of } \frac{1}{4} = 3 \text{ of } \frac{1}{4}$$

$$\text{Or, } \frac{1}{4} + \frac{2}{4} = \frac{1+2}{4} = \frac{3}{4}$$

$$\frac{18}{25} - \frac{3}{25} = \frac{18-3}{25} = \frac{15}{25} = \frac{3}{5}$$

FACT 2: We add and subtract unlike fractions, by adding and subtracting their equivalent like fractions.

The LCM of 6 and 9 is 18, therefore

$$\frac{5}{6} + \frac{7}{9} = \frac{5 \times 3}{6 \times 3} + \frac{7 \times 2}{9 \times 2} = \frac{15}{18} + \frac{14}{18} = \frac{29}{18}$$

The LCM of 15 and 18 is 90, therefore

$$\frac{4}{15} - \frac{7}{18} = \frac{4 \times 6 - 7 \times 5}{90} = \frac{24 - 35}{90} = -\frac{11}{90}$$

The LCM of 6, 14, 21 is 42, therefore

$$\frac{5}{6} + \frac{9}{14} - \frac{11}{21} = \frac{5 \times 7 + 9 \times 3 - 11 \times 2}{42} = \frac{35 + 27 - 22}{42} = \frac{40}{42} = \frac{20}{21}$$

FACT 2: Mixed numbers may be added or subtracted as improper fractions, or as mixed numbers.

$$2\frac{5}{8} + 3\frac{7}{12} = \frac{21}{8} + \frac{43}{12} = \frac{63 + 86}{24} = \frac{149}{24} = 6\frac{5}{24}$$

$$\begin{aligned} 3\frac{7}{12} - 2\frac{5}{8} &= (3 - 2) + \left(\frac{7}{12} - \frac{5}{8}\right) = 1 + \frac{14 - 15}{24} \\ &= 1 + \left(-\frac{1}{24}\right) = 1 - \frac{1}{24} = \frac{23}{24} \end{aligned}$$

1. Add and subtract the following. Reduce the result to the simplest form.

(a) $\frac{7}{18} + \frac{5}{18}$

(b) $\frac{5}{16} + \frac{3}{16}$

(c) $\frac{8}{45} + \frac{3}{45} + \frac{4}{45}$

(d) $\frac{4}{15} + \frac{7}{12}$

(e) $\frac{15}{16} + \frac{3}{24}$

(f) $\frac{7}{15} + \frac{3}{25} + \frac{11}{35}$

(g) $\frac{5}{12} - \frac{13}{14}$

(h) $\frac{21}{25} - \frac{29}{35}$

(i) $\frac{29}{55} - \frac{17}{33}$

Answer: (a) $\frac{2}{3}$ (b) $\frac{1}{2}$ (c) $\frac{1}{3}$ (d) $\frac{17}{20}$ (e) $\frac{17}{16}$ (f) $\frac{473}{525}$ (g) $-\frac{43}{84}$
(h) $\frac{2}{175}$ (i) $\frac{2}{165}$

2. Add and subtract the following. Reduce the result to the simplest form.

(a) $5\frac{4}{5} + 9\frac{3}{4}$

(b) $8\frac{5}{14} + 3\frac{3}{7}$

(c) $5\frac{2}{15} + 4\frac{1}{6} + 1\frac{3}{10}$

(d) $9\frac{3}{4} - 5\frac{4}{5}$

(e) $8\frac{5}{14} - 3\frac{3}{7}$

(f) $5\frac{2}{15} - 4\frac{1}{6}$

Answer: (a) $15\frac{11}{20}$ (b) $11\frac{11}{14}$ (c) $10\frac{3}{5}$ (d) $3\frac{19}{20}$ (e) $4\frac{13}{14}$ (f) $\frac{29}{30}$

End of Lesson